

NOVEMBER 11-14, 2019 Praiamar Natal Hotel & Convention Natal, RN-BRAZIL

# AN AIRCRAFT FUSELAGE FRACTURE ANALYSIS

Thiago A. A. Oliveira

Gilberto Gomes Eng.thiagoarnaud@gmail.com Ggomes2007@ University of Brasília Asa Norte, SQN 406, Bloco K, Ap. 208, Brasília, Brazil

## Abstract.

The continuum mechanics deals with the interaction between two bodies in order to analyze the stresses in the domain due to the contact load. In this way, to compute the stresses, it is considered each body as a semi-infinite in extent and having a plane surface. The Boundary Element Method (BEM) appears as a numerical technique for evaluating this type of problem. Using this technique, the boundary is discretized and the stresses are computed in the body domain. This paper consists of the multiscale analysis via Dual Boundary Element Method (DBEM) of fatigue life of aircraft fuselage plate. The macro analysis is evaluated through the stress field in the plate due to continuum mechanics. With this stress field, a micro element, composed by different distribution of cracks, is subjected to fatigue and analyzed by Dual Boundary Element Method (DBEM). This is accomplished using the software BemCracker2D obtaining fatigue life data in each crack increment. For this, advanced computational techniques were developed to evaluate the fracture mechanics behavior with the purpose of ensuring the integrity and the good functioning of the fuselage during its design lifespan.

Keywords: Dual Boundary Element Method, Multiscale Analysis, Fatigue, Aircraft Fuselage.

## **1** Introduction and Theory

From the technical point of view, it is sought to develop structures that are subject to combinations of external loads in a way that works in the usual situation and does not reach the respective Ultimate and Service Limit States [1]. For this, the knowledge of the stress field is a necessary condition to predict the behavior of these elements to avoid combinations that provoke a Limit State.

This paper analyzes the growth of aircraft fuselage subjected to external loads evaluated from the continuum mechanics [2]. In this way, a macro analysis of stresses in a fuselage plate is realized from the theory of the continuum, and after it is analyzed the behavior of the advance of the crack in this plate to evaluate fatigue, residual strength, Stress Intensity Factors, crack path and the deformations at every crack increase. The main objective is to evaluate from the continuum mechanics, cracked fuselage plates when subjected to continuum stresses. And, as specific objectives define crack propagation to obtain fracture mechanics parameters at each increment, such as: Stress Intensity Factors, number of loading cycles (fatigue), deformations and residual strength [3-12].

Fatigue is characterized by a cyclic loading process that causes progressive internal cumulative structural damage. After a certain number of cycles, the cracks can reach critical lengths that can make the structure unstable and, in some cases, lead to collapse. Admitting an elastic half-space body shown in Figure 1. External loads p(x) and q(x) act on the surface over the region from x = -a to x = b while the remainder of the body is free from loads. The stress components  $\sigma_x$ ,  $\sigma_y$ ,  $\tau_{xy}$  at all points through the solid are computed according to [13, 14] shown in Equations 1, 2 and 3.

$$\sigma_x = -\frac{2y}{\pi} \int_{-a}^{b} \frac{p(s)(x-s)^2}{((x-s)^2+y^2)^2} ds - \frac{2}{\pi} \int_{-a}^{b} \frac{q(s)(x-s)^3}{((x-s)^2+y)^2} ds$$
(1)

$$\sigma_y = -\frac{2y^3}{\pi} \int_{-a}^{b} \frac{p(s)}{((x-s)^2 + y^2)^2} ds - \frac{2y^2}{\pi} \int_{-a}^{b} \frac{q(s)(x-s)}{((x-s)^2 + y^2)^2} ds$$
(2)

$$\tau_{xy} = -\frac{2y^2}{\pi} \int_{-a}^{b} \frac{p(s)(x-s)}{((x-s)^2 + y^2)^2} ds - \frac{2y}{\pi} \int_{-a}^{b} \frac{q(s)(x-s)^2}{((x-s)^2 + y^2)^2} ds$$
(3)

## 2 Methodology

To achieve the objectives a routine was developed in Matlab to automate the stress field derived from continuum mechanics based on [13, 14] and showed in Eqs. 1, 2 and 3. From the stress field, it is analyzed the crack propagation in an infinitesimal element through Dual Boundary Element Method (DBEM) using BemCracker2D [15, 16] to obtain the required parameters. The DBEM has several advantages over other methods, mainly due to the simplified modelling of the cracked area, direct SIF calculation, reduced run times and accurate crack growth simulation [17-19].

#### 2.1 Macro element analysis

Figure 2 shows the model of the continuum problem to be analyzed. P and Q are normal and shear loads (MPa), respectively, and they can be non-uniform with lengths a and b (cm). With automation, loads P, Q (MPa) and a, b (cm) will assume the values in Table 1.



Figure 1: Model of the continuum mechanics



Figure 2: Macro element analysis

|                  |      | Table 1: Loading Series |     |    |
|------------------|------|-------------------------|-----|----|
|                  | Р    | Q                       | a   | b  |
| Loading Series 1 | 1000 | 0                       | -10 | 10 |
| Loading Series 2 | 1000 | 0                       | -10 | 0  |
| Loading Series 3 | 1000 | 1000                    | -10 | 10 |
| Loading Series 4 | 1000 | 1000                    | -10 | 0  |
| Loading Series 5 | 0    | 1000                    | -10 | 10 |
| Loading Series 6 | 0    | 1000                    | -10 | 0  |

#### 2.2 Micro element analysis

From the applied external load, the micro element is subject to stress in the directions x ( $\sigma_x$ ), y ( $\sigma_y$ ), and shear ( $\tau$ ), according to Figure 3. The value is obtained directly from the stress field of Eqs. 1, 2 and 3 considering a square of 1 cm of side located in the origin of the axis (x, y) of Figure 2. The preestablished crack has initial size of 0.1 cm.

### **3** Results

For the 1 x 1 cm micro element located at the axis origin shown in Figure 2 with a preexisting crack of 0.1 cm size subjected to the loading series 1, 2 and 3 presents the following stress fields indicated in Table 2. Applying these stress fields, the crack growth path and deformation results are shown in Figures 4, 5, 6, 7 and 8 for each loading series, respectively. The objective results of this work are shown in Tables 3, 4, 5, 6, 7 and 8 for each increment of crack of size 0.05 cm.

| Table 2: Stress field in the micro element (MPa) |              |            |        |  |  |  |
|--|--------------|------------|--------|--|--|--|
| Loads (MPa)                                      | $\sigma_{x}$ | $\sigma_y$ | τ      |  |  |  |
| Loading Series 1                                 | 999.87       | 1000.00    | 0.00   |  |  |  |
| Loading Series 2                                 | 499.94       | 500.00     | 318.31 |  |  |  |
| Loading Series 3                                 | 999.87       | 1000.00    | 999.87 |  |  |  |
| Loading Series 4                                 | 0.00         | 818.31     | 818.25 |  |  |  |
| Loading Series 5                                 | 0.00         | 0.00       | 999.87 |  |  |  |
| Loading Series 6                                 | 0.00         | 318.31     | 499.94 |  |  |  |



Figure 3: Micro element stress field







(a) Crack growth

(b) Deformed mesh





(a) Crack growth

(b) Deformed mesh

Figure 9: Fuselage behaviour Loading Series 6

|                    | Tuon                     | 5. Results for Loud | ing benes i      | Table 5: Results for Loading Series 1 |                   |  |  |  |  |
|--------------------|--------------------------|---------------------|------------------|---------------------------------------|-------------------|--|--|--|--|
| Crack<br>increment | <b>Residual Strength</b> | Load Cycles         | SIF I<br>(MPa√m) | SIF II<br>(MPa√m)                     | SIF-EQ<br>(MPa√m) |  |  |  |  |
| 0                  | 0                        | 0                   | 72.0622          | -1.99E-12                             | 1                 |  |  |  |  |
| 1                  | 0.755681                 | 52.49072            | 95.3607          | 3.87E-12                              | 1.32331           |  |  |  |  |
| 2                  | 0.599116                 | 74.93781            | 120.281          | 5.71E-12                              | 1.66913           |  |  |  |  |
| 3                  | 0.488826                 | 85.94768            | 147.419          | 3.49E-12                              | 2.04572           |  |  |  |  |
| 4                  | 0.407959                 | 91.83705            | 176.641          | 5.77E-12                              | 2.45122           |  |  |  |  |
|                    |                          |                     |                  |                                       |                   |  |  |  |  |

| Tabla | 3. | Posulte | for | Loading | Sorias | 1 |
|-------|----|---------|-----|---------|--------|---|
| Iadle | 31 | Results | IOT | Loading | Series | 1 |

CILAMCE 2019

Proceedings of the XLIbero-LatinAmerican Congress on Computational Methods in Engineering, ABMEC, Natal/RN, Brazil, November 11-14, 2019

| 5  | 0.347234 | 95.2159  | 207.532 | 9.02E-12 | 2.8799  |
|----|----------|----------|---------|----------|---------|
| 6  | 0.300915 | 97.27797 | 239.477 | 1.13E-11 | 3.3232  |
| 7  | 0.265304 | 98.61077 | 271.621 | 1.43E-11 | 3.76926 |
| 8  | 0.237991 | 99.52177 | 302.793 | 1.37E-11 | 4.20183 |
| 9  | 0.217433 | 100.1813 | 331.422 | 1.50E-11 | 4.59911 |
| 10 | 0.202717 | 100.6895 | 355.482 | 1.77E-11 | 0       |

| Table 4: Results for Loading Series 2 |                          |             |                  |                   |                   |
|---------------------------------------|--------------------------|-------------|------------------|-------------------|-------------------|
| Crack<br>increment                    | <b>Residual Strength</b> | Load cycles | SIF I<br>(MPa√m) | SIF II<br>(MPa√m) | SIF-EQ<br>(MPa√m) |
| 0                                     | 0                        | 0           | 36.0315          | -18.1037          | 1                 |
| 1                                     | 0.632296                 | 213.5569    | 73.2124          | -0.84049          | 1.58154           |
| 2                                     | 0.462899                 | 262.0393    | 99.9985          | -1.30234          | 2.1603            |
| 3                                     | 0.352915                 | 280.5802    | 131.166          | -1.60581          | 2.83354           |
| 4                                     | 0.269149                 | 288.3648    | 171.998          | -1.84885          | 3.71541           |
| 5                                     | 0.200498                 | 291.5654    | 230.901          | -2.1395           | 4.98759           |
| 6                                     | 0.143529                 | 292.7709    | 322.502          | -4.36119          | 6.96725           |
| 7                                     | 0.097036                 | 293.167     | 477.023          | -6.43715          | 10.3055           |
| 8                                     | 0.060193                 | 293.2741    | 769.099          | -7.71436          | 16.6134           |
| 9                                     | 0.032617                 | 293.2959    | 1419.23          | -16.9419          | 30.6589           |
| 10                                    | 0.015239                 | 293.2988    | 3037.89          | -30.1767          | 0                 |

Table 5: Results for Loading Series 3

| Crack     | <b>Posidual Strongth</b> | Load avalas | SIF I   | SIF II   | SIF-EQ  |
|-----------|--------------------------|-------------|---------|----------|---------|
| increment | Keshulai Strengtii       | Loau cycles | (MPa√m) | (MPa√m)  | (MPa√m) |
| 0         | 0                        | 0           | 72.0622 | -56.8669 | 1       |
| 1         | 0.625724                 | 12.19713    | 180.323 | -2.97177 | 1.59815 |
| 2         | 0.457403                 | 14.90175    | 246.723 | -3.10891 | 2.18626 |
| 3         | 0.349803                 | 15.9353     | 322.623 | -3.83444 | 2.85875 |
| 4         | 0.267462                 | 16.37333    | 421.986 | -3.77599 | 3.73886 |
| 5         | 0.199112                 | 16.55436    | 566.807 | 6.25634  | 5.02231 |
| 6         | 0.14179                  | 16.62216    | 795.865 | -11.0773 | 7.05268 |
| 7         | 0.094871                 | 16.644      | 1189.55 | -14.2971 | 10.5406 |
| 8         | 0.057789                 | 16.6497     | 1953    | -19.7375 | 17.3044 |
| 9         | 0.030269                 | 16.65079    | 3728.16 | -50.1163 | 33.037  |
| 10        | 0.014518                 | 16.65092    | 7772.58 | -112.564 | 0       |

Table 6: Results for Loading Series 4

| Crack<br>increment | <b>Residual Strength</b> | Load cycles | SIF I<br>(MPa√m) | SIF II<br>(MPa√m) | SIF-EQ<br>(MPa√m) |
|--------------------|--------------------------|-------------|------------------|-------------------|-------------------|
| 0                  | 0                        | 0           | -1.03274         | -46.5369          | 1                 |
| 1                  | 0.462376                 | 58.17771    | 114.887          | -3.02649          | 2.16274           |
| 2                  | 0.295878                 | 68.5422     | 179.651          | -2.94942          | 3.37977           |
| 3                  | 0.204239                 | 71.15631    | 260.284          | -3.69231          | 4.89622           |
| 4                  | 0.13787                  | 71.94176    | 385.551          | -6.18795          | 7.25323           |
| 5                  | 0.067592                 | 72.13344    | 786.415          | -12.7495          | 14.7947           |
| 6                  | 0.023467                 | 72.15182    | 2241.98          | -190.739          | 0                 |

| Table 7: Results for Loading Series 5 |                          |             |                  |                   |                   |
|---------------------------------------|--------------------------|-------------|------------------|-------------------|-------------------|
| Crack<br>increment                    | <b>Residual Strength</b> | Load cycles | SIF I<br>(MPa√m) | SIF II<br>(MPa√m) | SIF-EQ<br>(MPa√m) |
| 0                                     | 0                        | 0           | 5.26E-12         | -56.8669          | 1                 |
| 1                                     | 0.70775                  | 42.85735    | 92.7189          | -1.92455          | 1.41293           |
|                                       |                          |             |                  |                   |                   |

CILAMCE 2019

Proceedings of the XLIbero-LatinAmerican Congress on Computational Methods in Engineering, ABMEC, Natal/RN, Brazil, November 11-14, 2019

| 2  | 0.533504 | 66.2019  | 123.024 | -2.15511 | 1.8744  |
|----|----------|----------|---------|----------|---------|
| 3  | 0.41769  | 76.00086 | 157.148 | -2.50916 | 2.39412 |
| 4  | 0.323276 | 80.4276  | 203.06  | 2.88698  | 3.09333 |
| 5  | 0.241713 | 82.31484 | 271.616 | -2.89937 | 4.13714 |
| 6  | 0.172536 | 83.03004 | 380.51  | 4.25847  | 5.79588 |
| 7  | 0.116098 | 83.26259 | 565.396 | -8.58928 | 8.61339 |
| 8  | 0.071527 | 83.32451 | 917.885 | -9.54093 | 13.9807 |
| 9  | 0.038275 | 83.33682 | 1715.07 | -24.0966 | 26.1266 |
| 10 | 0.018188 | 83.33842 | 3609.64 | -40.1977 | 0       |
|    |          |          |         |          |         |

| Table 8: Results for Loading Series 6 |                    |             |          |          |         |
|---------------------------------------|--------------------|-------------|----------|----------|---------|
| Crack                                 | Desidual Strongth  | Load avalas | SIF I    | SIF II   | SIF-EQ  |
| increment                             | Kesiuuai Strengtii | Loau cycles | (MPa√m)  | (MPa√m)  | (MPa√m) |
| 0                                     | 0                  | 0.00E+00    | -0.40058 | -28.4337 | 1       |
| 1                                     | 0.535001           | 304.8075    | 60.9072  | -1.49791 | 1.86915 |
| 2                                     | 0.364999           | 387.2771    | 89.3236  | -1.39278 | 2.73973 |
| 3                                     | 0.271768           | 413.3057    | 119.968  | -1.84095 | 3.67961 |
| 4                                     | 0.20842            | 423.7156    | 156.436  | -2.29929 | 4.79799 |
| 5                                     | 0.158883           | 428.1429    | 205.199  | 3.25889  | 6.29394 |
| 6                                     | 0.115122           | 429.9184    | 283.155  | -5.37929 | 8.68646 |
| 7                                     | 0.074583           | 430.5016    | 437.111  | -7.33041 | 13.4078 |
| 8                                     | 0.040978           | 430.6351    | 795.669  | 11.3547  | 24.4033 |
| 9                                     | 0.018362           | 430.6535    | 1775.73  | -25.0611 | 54.4615 |
| 10                                    | 0.011113           | 430.6551    | 2045.23  | -1348.8  | 0       |

# 4 Conclusion

The crack paths follow the stress field presented in Table 2. Loading Series 1 result in a linear crack path due to the symmetrical stress field without shear stress. The crack growth in Loading Series 2 is similar to Loading Series 3 since the stress field is almost half of each other. Loading Series 4 and 6 represent a mixture of high and low magnitude of y-normal and shear stress, respectively. In the first case (LS4) the crack is deflected up. In Loading Series 5 there is the crack growth for pure shear stress.

Now, analyzing the numerical results of residual strength and load cycles in Tables 3 to 8 varying the size of application (LS1, LS3 and LS5 a=b=10 cm; to LS2, LS4 and LS6 a=0 cm and b=10 cm), comparing the Loading Series 1 and 2 (Tables 3 and 4, respectively) with pure external normal stress (P=1000 MPa), neglecting the external shear load. The residual strength reduces and the number of load cycles increases since the micro stress field reduces. For Loading Series 3 and 4 there is a mixture of normal and shear loads (P=1000 MPa and Q=1000 MPa), in these case the residual strength reduces and the number of load cycles increases, again, since the micro stress field reduces. For Loading Series 5 and 6 with pure external shear load (Q=1000 MPa) residual strength reduces and the number of load cycles increases, again, since the micro stress field reduces.

Analyzing the results of Stress Intensity Factors (SIF), there is a mixed mode fracture and higher values of  $\sigma_x$ ,  $\sigma_y$  and  $\tau$  increases SIF I and SIF II depending on the crack direction. For Loading Series 1, SIF I increases and SIF II is zero for each crack propagation. In all other Loading Series both SIF I and SIF II increase for each crack increment.

# Acknowledgements

The authors are grateful to the Brazilian National Research Council (CNPq), to the Brazilian Coordination for the Improvement of Higher Education (CAPES) and to Federal District Research Support Foundation (FAP-DF) for the supporting funds for this research.

# References

- Melchers, R. E. Structural Reliability Analysis and Prediction. 2. ed. Chichester, United Kingdom: Wiley. 456 p, 1999.
- [2] T. Oliveira, G. Gomes, F. Evangelista Jr. Multiscale aircraft fuselage fatigue analysis by the dual boundary element method. Multiscale aircraft fuselage fatigue analysis by the dual boundary element method. Engineering Analysis with Boundary Elements 104, 2019.
- [3] T. L. Anderson, Fracture mechanics: Fundamentals ans Applications, Boca, Ed., CRC Press, 2005.
- [4] D. Broek, The practical use of fracture mechanics, 1 ed., Netherlands: Kluwer Academic Publishers, 1988.
- [5] Z. P. Bazant and J. Planas, "Fracture and size effect in concrete and other quasibrittle materials," CRC Press, 1998.
- [6] P. C. Paris and F. Erdogan, "A critical analysis of crack propagation laws," Journal of basic engineering, nº 85, pp. 528-534, 1960.
- [7] A. A. Griffith, "The phenomena of rupture and flow in solids," Philosophical Transactions of the Royal Society of London, vol. 221, pp. 163-198, 1921.
- [8] A. A. Griffith, "The theory of rupture," First International Congress of Applied Mechanics, nº In C. B. Biezeno and J. M. Burgers, pp. 55-63, 1924.
- [9] G. R. Irwin, "Analysis of stress and strain near the end of a crack traversing a plate," Journal of Applied Mechanics, vol. 24, pp. 361-364, 1957.
- [10] G. R. Irwin, "Onset of Fast Crack Propagation in High Strength Steel and Aluminium Alloys," Sagamore Research Conferece Proceedings, vol. 2, pp. 289-305, 1956.
- [11] J. R. Rice, "A path independent integral and the approximate analysis of strain concentration by notches and cracks," Journal of applied mechanics, vol. 35, pp. 379-386, 1968.
- [12] J. R. Rice, "The mechanics of crack tip deformation and extension by fatigue," Syrup. on fatigue crack growth, n° ASTM-STP-415, 1967.
- [13] Johnson K. L. Continuum mechanic, Cambridge University Press, 1985.
- [14] Sackfield A., Hills D. A., Nowell D. *Mechanics of elastic continuums*, Butterworth-Heinemann, ISBN: 9781483291949, 45-48, 1993.
- [15] G. Gomes and M.A.M. Noronha, A B-Rep data structure and object GUI programming to implement 2D boundary elements. International Journal of Applied Mathematics and Computation. 4 (2012) 369-381.
- [16] G. Gomes, A. M. Delgado Neto and L. C. Wrobel, Modeling and view of 2D cracks using Dual Boundary Integral Equation (in Portuguese), Brasília/DF, Brazil, DF: Proceedings of the XXXVII Iberian Latin-American Congress on Computational Methods in Engineering, ABMEC/RIPE, 2(6), pp. 120-133, 2016, p. 113.
- [17] A. Portela, M. H. Aliabadi and D. P. Rooke, "The Dual Boundary Element Method: Efective implementation for crack problems," International Journal for Numerical Methods in Engineering, vol. 33, pp. 1269-1287, 1992.
- [18] A. Portela, M. H. Aliabadi and D. P. Rooke, "Dual boundary element analysis of cracked plates: singularity subtraction technique," International Journal of Fracture, vol. 55, pp. 17-28, 1993.
- [19] G. E. Blandford, A. R. Ingraffea and J. A. Liggett, "Two-Dimensional Stress Intensity Factor Computations Using the Boundary Element Method," International Journal Numerical Methods in Engineering, nº 17, pp. 387-404, 1981.